

Package ‘RobKF’

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Type Package

Title Innovative and/or Additive Outlier Robust Kalman Filtering

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Description Implements a series of robust Kalman filtering approaches. It implements the additive outlier robust filters of Ruckdeschel et al. (2014) <arXiv:1204.3358> and Agamenoni et al. (2018) <doi:10.1109/ICRA.2011.5979605>, the innovative outlier robust filter of Ruckdeschel et al. (2014) <arXiv:1204.3358>, as well as the innovative and additive outlier robust filter of Fisch et al. (2020) <arXiv:2007.03238>.

License GPL

Imports Rcpp (>= 1.0.2), Rdpack, ggplot2, reshape2, Matrix

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AORKF_huber	<i>A huberisation based additive outlier robust Kalman filter</i>
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Description

An additive outlier robust Kalman filter, based on the work by Ruckdeschel et al. (2014). This function assumes that the additions are potentially polluted by a heavy tailed process. The update equations are made robust to these via huberisation.

Usage

```
AORKF_huber(
  Y,
  mu_0,
  Sigma_0 = NULL,
  A,
  C,
  Sigma_Add,
  Sigma_Inn,
  h = 2,
  epsilon = 1e-06
)
```

Arguments

Y	A list of matrices containing the observations to be filtered.
mu_0	A matrix indicating the mean of the prior for the hidden states.
Sigma_0	A matrix indicating the variance of the prior for the hidden states. It defaults to the limit of the variance of the Kalman filter.
A	A matrix giving the updates for the hidden states.
C	A matrix mapping the hidden states to the observed states.
Sigma_Add	A positive definite matrix giving the additive noise covariance.
Sigma_Inn	A positive definite matrix giving the innovative noise covariance.
h	A numeric giving the huber threshold. It defaults to 2.
epsilon	A positive numeric giving the precision to which the limit of the covariance is to be computed. It defaults to 0.000001.

Value

An rkf S3 class.

References

Ruckdeschel P, Spangl B, Pupashenko D (2014). “Robust Kalman tracking and smoothing with propagating and non-propagating outliers.” *Statistical Papers*, **55**(1), 93–123.

Examples

```
library(RobKF)

set.seed(2019)

A = matrix(c(1), nrow = 1, ncol = 1)
C = matrix(c(1), nrow = 1, ncol = 1)

Sigma_Inn = diag(1,1)*0.01
Sigma_Add = diag(1,1)

mu_0 = matrix(0,nrow=1,ncol=1)

Y_list = Generate_Data(1000,A,C,Sigma_Add,Sigma_Inn,mu_0,anomaly_loc = c(100,400,700),
                      anomaly_type = c("Add","Add","Add"),anomaly_comp = c(1,1,1),
                      anomaly_strength = c(10,10,10))

Output = AORKF_huber(Y_list,mu_0,Sigma_0=NULL,A,C,Sigma_Add,Sigma_Inn)

plot(Output,conf_level = 0.9999)
```

AORKF_t

A t-distribution based additive outlier robust Kalman filter

Description

An additive outlier robust Kalman filter, based on the work by Agamennoni et al. (2018). This function assumes that the additions are potentially polluted by a heavy tailed process, which is approximated by a t-distribution. Variational inference is used to approximate the posterior.

Usage

```
AORKF_t(
  Y,
  mu_0,
  Sigma_0 = NULL,
  A,
  C,
  Sigma_Add,
  Sigma_Inn,
  s = 2,
  epsilon = 1e-06
)
```

Arguments

Y	A list of matrices containing the observations to be filtered.
mu_0	A matrix indicating the mean of the prior for the hidden states.
Sigma_0	A matrix indicating the Variance of the prior for the hidden states. It defaults to the limit of the variance of the Kalman filter.
A	A matrix giving the updates for the hidden states.
C	A matrix mapping the hidden states to the observed states.
Sigma_Add	A positive definite matrix giving the additive noise covariance.
Sigma_Inn	A positive definite matrix giving the innovative noise covariance.
s	A numeric giving the shape of the t-distribution to be considered. It defaults to 2.
epsilon	A positive numeric giving the precision to which the limit of the covariance, and the variational inferences is to be computed. It defaults to 0.000001.

Value

An rkf S3 class.

References

Agamennoni G, Nieto JJ, Nebot EM (2011). "An outlier-robust Kalman filter." In *2011 IEEE International Conference on Robotics and Automation*, 1551–1558. IEEE.

Examples

```
library(RobKF)

set.seed(2019)

A = matrix(c(1), nrow = 1, ncol = 1)
C = matrix(c(1), nrow = 1, ncol = 1)

Sigma_Inn = diag(1,1)*0.01
Sigma_Add = diag(1,1)

mu_0 = matrix(0,nrow=1,ncol=1)

Y_list = Generate_Data(1000,A,C,Sigma_Add,Sigma_Inn,mu_0,anomaly_loc = c(100,400,700),
                      anomaly_type = c("Add","Add","Add"),anomaly_comp = c(1,1,1),
                      anomaly_strength = c(10,10,10))

Output = AORKF_t(Y_list,mu_0,Sigma_0=NULL,A,C,Sigma_Add,Sigma_Inn)

plot(Output,conf_level = 0.9999)
```

 Generate_Data

Simulate data from a Kalman model

Description

This function simulates data obeying a Kalman model whilst allowing the user to add innovative and additive anomalies.

Usage

```
Generate_Data(
  n,
  A,
  C,
  Sigma_Add,
  Sigma_Inn,
  mu_0 = NULL,
  anomaly_loc = integer(0),
  anomaly_type = character(0),
  anomaly_comp = integer(0),
  anomaly_strength = NULL
)
```

Arguments

n	A positive integer giving the number of observations desired
A	A matrix giving the updates for the hidden states.
C	A matrix mapping the hidden states to the observed states.
Sigma_Add	A positive definite diagonal matrix giving the additive noise covariance.
Sigma_Inn	A positive definite diagonal matrix giving the innovative noise covariance.
mu_0	A matrix indicating the mean of the prior for the hidden states. It defaults to a zero-vector.
anomaly_loc	A vector of integers giving the locations of anomalies.
anomaly_type	A vector of strings, either "Add" or "Inn" indicating whether the anomaly is additive or innovative.
anomaly_comp	A vector of integers giving the component affected by the anomalies.
anomaly_strength	A vector of numerics giving the strength of the anomalies (in sigmas).

Value

A list of matrices, each corresponding to an observation.

Examples

```

library(RobKF)
library(ggplot2)

set.seed(2018)

A = diag(2)*0.99
A[1,2] = -0.05
C = matrix(c(10,0.1),nrow=1)
mu = matrix(c(0,0),nrow=2)
Sigma_Inn = diag(c(1,0.01)*0.00001,nrow=2)
Sigma_Add = diag(c(1)*0.1,nrow=1)

Y_list = Generate_Data(100,A,C,Sigma_Add,Sigma_Inn, mu_0 = mu, anomaly_loc = c(10,30,50),
                      anomaly_type = c("Inn","Add","Inn"),
                      anomaly_comp = c(1,1,2), anomaly_strength = c(400,-10,3000))

qplot(1:100,unlist(Y_list),xlab="time",ylab="observation")+theme_minimal()

```

 IOAORKF

An innovative and additive outlier robust Kalman filter

Description

An implementation of Computationally Efficient Bayesian Anomaly detection by Sequential Sampling (CE-BASS) by Fisch et al. (2020). This function assumes that both the innovations and additions are potentially polluted by a heavy tailed process, which is approximated by a t-distribution. To approximate the posterior, particles for the precision (inverse variance) are sampled using a robust approximation to the posterior. Conditionally on those samples, the classical Kalman updates are used.

Usage

```

IOAORKF(
  Y,
  mu_0,
  Sigma_0 = NULL,
  A,
  C,
  Sigma_Add,
  Sigma_Inn,
  Particles,
  Descendants = 1,
  s = 2,
  anom_add_prob = NULL,

```

```

    anom_inn_prob = NULL,
    epsilon = 1e-06,
    horizon_matrix = NULL
)

```

Arguments

<code>Y</code>	A list of matrices containing the observations to be filtered.
<code>mu_0</code>	A matrix indicating the mean of the prior for the hidden states.
<code>Sigma_0</code>	A matrix indicating the variance of the prior for the hidden states. It defaults to the limit of the variance of the Kalman filter.
<code>A</code>	A matrix giving the updates for the hidden states.
<code>C</code>	A matrix mapping the hidden states to the observed states.
<code>Sigma_Add</code>	A positive definite diagonal matrix giving the additive noise covariance.
<code>Sigma_Inn</code>	A positive definite diagonal matrix giving the innovative noise covariance.
<code>Particles</code>	An integer giving the number of particles to be maintained at each step. More particles lead to more accuracy, but also require more memory and CPU time. The parameter should be at least $p + q + 1$, where p is the dimension of the observations and q the dimension of the hidden states.
<code>Descendants</code>	An integer giving the number of descendants to be sampled for each of the possible anomalies. Increasing Descendants leads to higher accuracy but also higher memory and CPU requirements. The default value is 1.
<code>s</code>	A numeric giving the shape of the t-distribution to be considered. It defaults to 2.
<code>anom_add_prob</code>	A vector of probabilities with length equal to the dimension of the observations giving the probabilities of additive outliers in each of the components. It defaults to 1/10000.
<code>anom_inn_prob</code>	A vector of probabilities with length equal to the dimension of the hidden state giving the probabilities of innovative outliers in each of the components. It defaults to 1/10000.
<code>epsilon</code>	A positive numeric giving the precision to which the limit of the covariance is to be computed. It defaults to 0.000001.
<code>horizon_matrix</code>	A matrix of 0s and 1s giving the horizon's at which innovative particles are to be resampled. It defaults to a k by q matrix, where k is the number of observations required for observability of the system and q is the dimension of the hidden states.

Value

An `ioorkf` S3 class.

References

Fisch A, Eckley IA, Fearnhead P (2020). "Innovative And Additive Outlier Robust Kalman Filtering With A Robust Particle Filter." *arXiv preprint arXiv:2007.03238*.

Examples

```

library(RobKF)

set.seed(2018)

A = diag(2)*0.99
A[1,2] = -0.05
C = matrix(c(10,0.1),nrow=1)
mu = matrix(c(0,0),nrow=2)
Sigma_Inn = diag(c(1,0.01)*0.00001,nrow=2)
Sigma_Add = diag(c(1)*0.1,nrow=1)

Y_list = Generate_Data(100,A,C,Sigma_Add,Sigma_Inn, mu_0 = mu, anomaly_loc = c(10,30,50),
                      anomaly_type = c("Inn","Add","Inn"),
                      anomaly_comp = c(1,1,2), anomaly_strength = c(400,-10,3000))

horizon_matrix = matrix(1,nrow = 3 ,ncol = 2)

Particle_List = IOAORKF(Y_list,mu,Sigma_0=NULL,A,C,Sigma_Add,Sigma_Inn,Particles=20,
                      horizon_matrix=horizon_matrix)

plot(Particle_List)
summary(Particle_List)

```

 IORKF_huber

A huberisation based innovative outlier robust Kalman filter

Description

An innovative outlier robust Kalman filter, based on the work by Ruckdeschel et al. (2014). This function assumes that the innovations are potentially polluted by a heavy tailed process. The update equations are made robust to these via huberisation.

Usage

```

IORKF_huber(
  Y,
  mu_0,
  Sigma_0 = NULL,
  A,
  C,
  Sigma_Add,
  Sigma_Inn,
  h = 2,
  epsilon = 1e-06
)

```


Arguments

Y	A list of matrices containing the observations to be filtered.
mu_0	A matrix indicating the mean of the prior for the hidden states.
Sigma_0	A matrix indicating the variance of the prior for the hidden states. It defaults to the limit of the variance of the Kalman filter.
A	A matrix giving the updates for the hidden states.
C	A matrix mapping the hidden states to the observed states.
Sigma_Add	A positive definite matrix giving the additive noise covariance.
Sigma_Inn	A positive definite matrix giving the innovative noise covariance.
h	A numeric giving the huber threshold. It defaults to 2.
epsilon	A positive numeric giving the precision to which the limit of the covariance is to be computed. It defaults to 0.000001.

Value

An rkf S3 class.

References

Ruckdeschel P, Spangl B, Pupashenko D (2014). “Robust Kalman tracking and smoothing with propagating and non-propagating outliers.” *Statistical Papers*, **55**(1), 93–123.

Examples

```
library(RobKF)

set.seed(2019)

A = matrix(c(1), nrow = 1, ncol = 1)
C = matrix(c(1), nrow = 1, ncol = 1)

Sigma_Inn = diag(1,1)*0.01
Sigma_Add = diag(1,1)

mu_0 = matrix(0,nrow=1,ncol=1)

Y_list = Generate_Data(1000,A,C,Sigma_Add,Sigma_Inn,mu_0,anomaly_loc = c(100,400,700),
                      anomaly_type = c("Inn","Inn","Inn"),anomaly_comp = c(1,1,1),
                      anomaly_strength = c(50,80,-100))

Output = IORKF_huber(Y_list,mu_0,Sigma_0=NULL,A,C,Sigma_Add,Sigma_Inn,h=2)

plot(Output,conf_level = 0.9999)
```

 KF *The classical Kalman filter*

Description

The classical Kalman filter.

Usage

```
KF(Y, mu_0, Sigma_0 = NULL, A, C, Sigma_Add, Sigma_Inn, epsilon = 1e-06)
```

Arguments

Y	A list of matrices containing the observations to be filtered.
mu_0	A matrix indicating the mean of the prior for the hidden states.
Sigma_0	A matrix indicating the variance of the prior for the hidden states. It defaults to the limit of the variance of the Kalman filter.
A	A matrix giving the updates for the hidden states.
C	A matrix mapping the hidden states to the observed states.
Sigma_Add	A positive definite matrix giving the additive noise covariance.
Sigma_Inn	A positive definite matrix giving the innovative noise covariance.
epsilon	A positive numeric giving the precision to which the limit of the covariance is to be computed. It defaults to 0.000001.

Value

An rkf S3 class.

References

Kalman RE (1960). "A New Approach to Linear Filtering and Prediction Problems." *Transactions of the ASME—Journal of Basic Engineering*, **82**(Series D), 35–45.

Examples

```
library(RobKF)

set.seed(2019)

A = matrix(c(1), nrow = 1, ncol = 1)
C = matrix(c(1), nrow = 1, ncol = 1)

Sigma_Inn = diag(1,1)*0.01
Sigma_Add = diag(1,1)

mu_0 = matrix(0,nrow=1,ncol=1)
```

```

Y_list = Generate_Data(1000,A,C,Sigma_Add,Sigma_Inn,mu_0)

Output = KF(Y_list,mu_0,Sigma_0=NULL,A,C,Sigma_Add,Sigma_Inn)

plot(Output)

```

plot

plot

Description

A function to plot the output produced by [AORKF_t](#), [AORKF_huber](#), [IORKF_huber](#) or [IOAORKF](#). One can specify a time during the run for which the output should be displayed.

Usage

```

## S3 method for class 'ioaorkf'
plot(x, time = NULL, horizon = NULL, subset = NULL, ...)

## S3 method for class 'rkf'
plot(x, time = NULL, subset = NULL, conf_level = 0.95, ...)

```

Arguments

x	An instance of an <code>ioaorkf</code> or <code>rkf</code> S3 class.
time	A positive integer giving the time at which the output is to be displayed. It defaults to the number of observations.
horizon	A positive integer giving the smoothing horizon that is to be used. It must be at least equal to the number of rows of the horizonmatrix used to obtain the <code>ioaorkf</code> object.
subset	A list of integers indicating the components of observations which are to be plotted.
...	Ignored.
conf_level	A probability between 0 and 1 giving the confidence level at which the series are to be tested against anomalies. It defaults to 0.95.

Value

A `ggplot` object.

print	<i>print</i>
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Description

A function to print the output produced by [AORKF_t](#), [AORKF_huber](#), [IORKF_huber](#) or [IOAORKF](#). One can specify a time during the run for which the output should be displayed.

Usage

```
## S3 method for class 'ioaorkf'
print(x, time = NULL, horizon = NULL, ...)

## S3 method for class 'rkf'
print(x, time = NULL, conf_level = 0.95, ...)
```

Arguments

x	An instance of an ioaorkf or rkf S3 class.
time	A positive integer giving the time at which the output is to be displayed. It defaults to the number of observations.
horizon	A positive integer giving the smoothing horizon that is to be used. It must be at least equal to the number of rows of the horizonmatrix used to obtain the ioaorkf object.
...	Ignored.
conf_level	A probability between 0 and 1 giving the confidence level at which the series are to be tested against anomalies. It defaults to 0.95.

summary	<i>Summary</i>
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Description

A function to summarise the output produced by [AORKF_t](#), [AORKF_huber](#), [IORKF_huber](#), or [IOAORKF](#). One can specify a time during the run for which the output should be displayed.

Usage

```
## S3 method for class 'ioaorkf'
summary(object, time = NULL, horizon = NULL, ...)

## S3 method for class 'rkf'
summary(object, time = NULL, conf_level = 0.95, ...)
```

Arguments

object	An instance of an <code>ioaorkf</code> or <code>rkf</code> S3 class.
time	A positive integer giving the time at which the output is to be displayed. It defaults to the number of observations.
horizon	A positive integer giving the smoothing horizon that is to be used. It must be at least equal to the number of rows of the <code>horizonmatrix</code> used to obtain the <code>ioaorkf</code> object.
...	Ignored
conf_level	A probability between 0 and 1 giving the confidence level at which the series are to be tested against anomalies. It defaults to 0.95.

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