

# Package ‘wv’

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**Title** Wavelet Variance

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**Description** Provides a series of tools to compute and plot quantities related to classical and robust wavelet variance for time series and regular lattices. More details can be found, for example, in Serroukh, A., Walden, A.T., & Percival, D.B. (2000) <doi:10.2307/2669537> and Guerrier, S. & Molinari, R. (2016) <arXiv:1607.05858>.

**Depends** R (>= 3.5.0)

**License** AGPL-3

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ACF

*Auto-Covariance and Correlation Functions***Description**

The ACF function computes the estimated autocovariance or autocorrelation for both univariate and multivariate cases.

**Usage**

```
ACF(x, lagmax = 0, cor = TRUE, demean = TRUE)
```

**Arguments**

x	A matrix with dimensions $N \times S$ or N observations and S processes
lagmax	A integer indicating the max lag.
cor	A bool indicating whether the correlation (TRUE) or covariance (FALSE) should be computed.
demean	A bool indicating whether the data should be detrended (TRUE) or not (FALSE)

**Details**

lagmax default is  $10 * \log_{10}(N/m)$  where  $N$  is the number of observations and  $m$  is the number of series being compared. If lagmax supplied is greater than the number of observations, then one less than the total will be taken.

**Value**

An array of dimensions  $N \times S \times S$ .

**Author(s)**

Yunxiang Zhang

**Examples**

```
# Get Autocorrelation
m = ACF(datasets::AirPassengers)

# Get Autocovariance and do not remove trend from signal
m = ACF(datasets::AirPassengers, cor = FALSE, demean = FALSE)
```

---

adis\_wv

*Wavelet variance of IMU Data from an ADIS 16405 sensor*

---

**Description**

This data set contains wavelet variance of gyroscope and accelerometer data from an ADIS 16405 sensor.

**Usage**

adis\_wv

**Format**

A list of the following elements:

- "sensor": Name of the sensor.
- "freq": The frequency at which the error signal is measured.
- "n": Sample size of the data.
- "type": The types of sensors considered in the data.
- "axis": The axes of sensors considered in the data.
- "wvar": A list containing the computed wavelet variance based on the data.

**Source**

The IMU data comes from Department of Geomatics Engineering, University of Calgary.

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ar1_to_wv	<i>AR(1) process to WV</i>
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---

**Description**

This function computes the Haar WV of an AR(1) process

**Usage**

```
ar1_to_wv(phi, sigma2, tau)
```

**Arguments**

phi	A double that is the phi term of the AR(1) process
sigma2	A double corresponding to variance of AR(1) process
tau	A vec containing the scales e.g. $2^\tau$

**Details**

This function is significantly faster than its generalized counter part [arma\\_to\\_wv](#).

**Value**

A vec containing the wavelet variance of the AR(1) process.

**Process Haar Wavelet Variance Formula**

The Autoregressive Order 1 (AR(1)) process has a Haar Wavelet Variance given by:

$$\frac{2\sigma^2 \left( 4\phi^{\frac{\tau_j}{2}+1} - \phi^{\tau_j+1} - \frac{1}{2}\phi^2\tau_j + \frac{\tau_j}{2} - 3\phi \right)}{(1-\phi)^2 (1-\phi^2)\tau_j^2}$$

**See Also**

[arma\\_to\\_wv](#), [arma11\\_to\\_wv](#)

---

arma11_to_wv	<i>ARMA(1,1) to WV</i>
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---

**Description**

This function computes the WV (haar) of an Autoregressive Order 1 - Moving Average Order 1 (ARMA(1,1)) process.

**Usage**

```
arma11_to_wv(phi, theta, sigma2, tau)
```

**Arguments**

phi	A double corresponding to the autoregressive term.
theta	A double corresponding to the moving average term.
sigma2	A double the variance of the process.
tau	A vec containing the scales e.g. $2^\tau$

**Details**

This function is significantly faster than its generalized counter part [arma\\_to\\_wv](#)

**Value**

A vec containing the wavelet variance of the ARMA(1,1) process.

**Process Haar Wavelet Variance Formula**

The Autoregressive Order 1 and Moving Average Order 1 (ARMA(1,1)) process has a Haar Wavelet Variance given by:

$$\nu_j^2(\phi, \theta, \sigma^2) = -\frac{2\sigma^2 \left( -\frac{1}{2}(\theta + 1)^2 (\phi^2 - 1) \tau_j - (\theta + \phi)(\theta\phi + 1) \left( \phi^{\tau_j} - 4\phi^{\frac{\tau_j}{2}} + 3 \right) \right)}{(\phi - 1)^3 (\phi + 1) \tau_j^2}$$

**See Also**

[arma\\_to\\_wv](#)

arma\_to\_wv

*ARMA process to WV***Description**

This function computes the Haar Wavelet Variance of an ARMA process

**Usage**

```
arma_to_wv(ar, ma, sigma2, tau)
```

**Arguments**

ar	A vec containing the coefficients of the AR process
ma	A vec containing the coefficients of the MA process
sigma2	A double containing the residual variance
tau	A vec containing the scales e.g. $2^\tau$

**Details**

The function is a generic implementation that requires a stationary theoretical autocorrelation function (ACF) and the ability to transform an ARMA( $p,q$ ) process into an MA( $\infty$ ) (e.g. infinite MA process).

**Value**

A vec containing the wavelet variance of the ARMA process.

**Process Haar Wavelet Variance Formula**

The Autoregressive Order  $p$  and Moving Average Order  $q$  (ARMA( $p,q$ )) process has a Haar Wavelet Variance given by:

$$\frac{\tau_j \left[ 1 - \rho \left( \frac{\tau_j}{2} \right) \right] + 2 \sum_{i=1}^{\frac{\tau_j}{2} - 1} i \left[ 2\rho \left( \frac{\tau_j}{2} - i \right) - \rho(i) - \rho(\tau_j - i) \right]}{\tau_j^2} \sigma_X^2$$

where  $\sigma_X^2$  is given by the variance of the ARMA process. Furthermore, this assumes that stationarity has been achieved as it directly

**See Also**

[ARMAtoMA\\_cpp](#), [ARMAacf\\_cpp](#), and [arma11\\_to\\_wv](#)

---

av_ar1	<i>Calculate Theoretical Allan Variance for Stationary First-Order Autoregressive (AR1) Process</i>
--------	---

---

### Description

This function allows us to calculate the theoretical allan variance for stationary first-order autoregressive (AR1) process.

### Usage

```
av_ar1(n, phi, sigma2)
```

### Arguments

n	An integer value for the size of the cluster.
phi	A double value for the autocorrection parameter $\phi$ .
sigma2	A double value for the variance parameter $\sigma^2$ .

### Value

A double indicating the theoretical allan variance for AR1 process.

### Note

This function is based on the calculation of the theoretical allan variance for stationary AR1 process raised in "Allan Variance of Time Series Models for Measurement Data" by Nien Fan Zhang.) This calculation is fundamental and necessary for the study in "A Study of the Allan Variance for Constant-Mean Non-Stationary Processes" by Xu et al. (IEEE Signal Processing Letters, 2017).

### Author(s)

Yuming Zhang

### Examples

```
av1 = av_ar1(n = 5, phi = 0.9, sigma2 = 1)
av2 = av_ar1(n = 8, phi = 0.5, sigma2 = 2)
```

---

av_wn	<i>Calculate Theoretical Allan Variance for Stationary White Noise Process</i>
-------	--

---

### Description

This function allows us to calculate the theoretical allan variance for stationary white noise process.

### Usage

```
av_wn(sigma2, n)
```

### Arguments

sigma2	A double value for the variance parameter $\sigma^2$ .
n	An integer value for the size of the cluster.

### Value

A double indicating the theoretical allan variance for the white noise process.

### Note

This function is based on the calculation of the theoretical allan variance for stationary white noise process raised in "Allan Variance of Time Series Models for Measurement Data" by Nien Fan Zhang. This calculation is fundamental and necessary for the study in "A Study of the Allan Variance for Constant-Mean Non-Stationary Processes" by Xu et al. (IEEE Signal Processing Letters, 2017).

### Author(s)

Yuming Zhang

### Examples

```
av1 = av_wn(sigma2 = 1, n = 5)
av2 = av_wn(sigma2 = 2, n = 8)
```



**Description**

Displays plots of multiple wavelet variances of different time series accounting for CI values.

**Usage**

```
compare_wvar(
  ...,
  split = FALSE,
  add_legend = TRUE,
  units = NULL,
  xlab = NULL,
  ylab = NULL,
  main = NULL,
  col_wv = NULL,
  col_ci = NULL,
  nb_ticks_x = NULL,
  nb_ticks_y = NULL,
  legend_position = NULL,
  ci_wv = NULL,
  point_cex = NULL,
  point_pch = NULL,
  names = NULL,
  cex_labels = 0.8
)
```

**Arguments**

...	One or more time series objects.
split	A boolean that, if TRUE, arranges the plots into a matrix-like format.
add_legend	A boolean that, if TRUE, adds a legend to the plot.
units	A string that specifies the units of time plotted on the x axes. Note: This argument will not be used if xlab is specified.
xlab	A string that gives a title for the x axes.
ylab	A string that gives a title for the y axes.
main	A string that gives an overall title for the plot.
col_wv	A string that specifies the color of the wavelet variance lines.
col_ci	A string that specifies the color of the confidence interval shade.
nb_ticks_x	An integer that specifies the maximum number of ticks for the x-axis.
nb_ticks_y	An integer that specifies the maximum number of ticks for the y-axis.

legend_position	A string that specifies the position of the legend (use legend_position = NA to remove legend).
ci_wv	A boolean that determines whether confidence interval polygons will be drawn.
point_cex	A double that specifies the size of each symbol to be plotted.
point_pch	A double that specifies the symbol type to be plotted.
names	A string that specifies the name of the WVAR objects.
cex_labels	A double that specifies the magnification of the labels (x and y).

**Author(s)**

Stephane Guerrier and Justin Lee

**Examples**

```
set.seed(999)
n = 10^4
Xt = arima.sim(n = n, list(ar = 0.10))
Yt = arima.sim(n = n, list(ar = 0.35))
Zt = arima.sim(n = n, list(ar = 0.70))
Wt = arima.sim(n = n, list(ar = 0.95))

wv_Xt = wvar(Xt)
wv_Yt = wvar(Yt)
wv_Zt = wvar(Zt)
wv_Wt = wvar(Wt)

compare_wvar(wv_Xt, wv_Yt, wv_Zt, wv_Wt)
```

---

compare\_wvar\_no\_split *Combined Plot Comparison Between Multiple Wavelet Variances*

---

**Description**

This is a helper function for the compare\_var() function. This method accepts the same set of arguments as compare\_wvar and returns a single plot that compares multiple wavelet variances of different time series accounting for CI values.

**Usage**

```
compare_wvar_no_split(graph_details)
```

**Arguments**

graph\_details List of inputs

**Author(s)**

Stephane Guerrier, Justin Lee, and Nathanael Claussen

---

compare_wvar_split	<i>Multi-Plot Comparison Between Multiple Wavelet Variances</i>
--------------------	---

---

**Description**

This is a helper function for the `compare_var()` function. This method accepts the same set of arguments as `compare_wvar` and returns a comparison of multiple wavelet variances of different time series accounting for CI values as a set of different plots.

**Usage**

```
compare_wvar_split(graph_details)
```

**Arguments**

`graph_details` List of inputs

**Author(s)**

Stephane Guerrier, Justin Lee, and Nathanael Claussen

---

dr_to_wv	<i>Drift to WV</i>
----------	--------------------

---

**Description**

This function compute the WV (haar) of a Drift process

**Usage**

```
dr_to_wv(omega, tau)
```

**Arguments**

`omega` A double corresponding to the slope of the drift  
`tau` A vec containing the scales e.g.  $2^T$

**Value**

A vec containing the wavelet variance of the drift.

**Process Haar Wavelet Variance Formula**

The Drift (DR) process has a Haar Wavelet Variance given by:

$$\nu_j^2(\omega) = \frac{\tau_j^2 \omega^2}{16}$$

---

`dwt`*Discrete Wavelet Transform*

---

**Description**

Calculation of the coefficients for the discrete wavelet transformation

**Usage**

```
dwt(x, nlevels = floor(log2(length(x))), filter = "haar")
```

**Arguments**

<code>x</code>	A vector with dimensions $N \times 1$ .
<code>nlevels</code>	A integer indicating the $J$ levels of decomposition.
<code>filter</code>	A string indicating the filter name

**Details**

Performs a level  $J$  decomposition of the time series using the pyramid algorithm. The default  $J$  is determined by  $\text{floor}(\log_2(\text{length}(x)))$

**Value**

A field<vec> that contains the wavelet coefficients for each decomposition level

**Author(s)**

James Balamuta, Justin Lee and Stephane Guerrier

**Examples**

```
set.seed(999)
x = rnorm(2^8)
ret = dwt(x)

summary(ret)

plot(ret)
```

---

imar\_wv

*Wavelet variance of IMU Data from IMAR Gyroscopes*

---

**Description**

This data set contains wavelet variance of IMAR gyroscopes data.

**Usage**

imar\_wv

**Format**

A list of the following elements:

- "sensor": Name of the sensor.
- "freq": The frequency at which the error signal is measured.
- "n": Sample size of the data.
- "type": The types of sensors considered in the data.
- "axis": The axes of sensors considered in the data.
- "wvar": A list containing the computed wavelet variance based on the data.

**Source**

The IMU data comes from Geodetic Engineering Laboratory (TOPO) and Swiss Federal Institute of Technology Lausanne (EPFL).

---

kvh1750\_wv

*Wavelet variance of IMU Data from a KVH1750 IMU sensor*

---

**Description**

This data set contains wavelet variance of gyroscope and accelerometer data from an KVH1750 sensor.

**Usage**

kvh1750\_wv

**Format**

A list of the following elements:

- "sensor": Name of the sensor.
- "freq": The frequency at which the error signal is measured.
- "n": Sample size of the data.
- "type": The types of sensors considered in the data.
- "axis": The axes of sensors considered in the data.
- "wvar": A list containing the computed wavelet variance based on the data.

**Source**

The IMU data comes from Department of Geomatics Engineering, University of Calgary.

---

In200\_wv

*Wavelet variance of IMU Data from a LN200 sensor*

---

**Description**

This data set contains wavelet variance of LN200 gyroscope and accelerometer data.

**Usage**

In200\_wv

**Format**

A list of the following elements:

- "sensor": Name of the sensor.
- "freq": The frequency at which the error signal is measured.
- "n": Sample size of the data.
- "type": The types of sensors considered in the data.
- "axis": The axes of sensors considered in the data.
- "wvar": A list containing the computed wavelet variance based on the data.

**Source**

The IMU data comes from Geodetic Engineering Laboratory (TOPO) and Swiss Federal Institute of Technology Lausanne (EPFL).

---

`ma1_to_wv`*Moving Average Order 1 (MA(1)) to WV*

---

### Description

This function computes the WV (haar) of a Moving Average order 1 (MA1) process.

### Usage

```
ma1_to_wv(theta, sigma2, tau)
```

### Arguments

<code>theta</code>	A double corresponding to the moving average term.
<code>sigma2</code>	A double the variance of the process.
<code>tau</code>	A vec containing the scales e.g. $2^\tau$

### Details

This function is significantly faster than its generalized counter part [arma\\_to\\_wv](#).

### Value

A vec containing the wavelet variance of the MA(1) process.

### Process Haar Wavelet Variance Formula

The Moving Average Order 1 (MA(1)) process has a Haar Wavelet Variance given by:

$$\nu_j^2(\theta, \sigma^2) = \frac{\left( (\theta + 1)^2 \tau_j - 6\theta \right) \sigma^2}{\tau_j^2}$$

### See Also

[arma\\_to\\_wv](#), [arma11\\_to\\_wv](#)

---

`modwt`*Maximum Overlap Discrete Wavelet Transform*

---

**Description**

Calculates the coefficients for the discrete wavelet transformation

**Usage**

```
modwt(x, nlevels = floor(log2(length(x) - 1)), filter = "haar")
```

**Arguments**

<code>x</code>	A vector with dimensions $N \times 1$ .
<code>nlevels</code>	A integer indicating the $J$ levels of decomposition.
<code>filter</code>	A string indicating the filter name

**Details**

Performs a level  $J$  decomposition of the time series using the pyramid algorithm. The default  $J$  is determined by  $\text{floor}(\log_2(\text{length}(x)))$

**Value**

A field<vec> that contains the wavelet coefficients for each decomposition level

**Author(s)**

James Balamuta, Justin Lee and Stephane Guerrier

**Examples**

```
set.seed(999)
x = rnorm(100)
ret = modwt(x)

summary(ret)

plot(ret)
```



---

navchip_wv	<i>Wavelet variance of IMU Data from a navchip sensor</i>
------------	---

---

**Description**

This data set contains wavelet variance of gyroscope and accelerometer data from a navchip sensor.

**Usage**

navchip\_wv

**Format**

A list of the following elements:

- "sensor": Name of the sensor.
- "freq": The frequency at which the error signal is measured.
- "n": Sample size of the data.
- "type": The types of sensors considered in the data.
- "axis": The axes of sensors considered in the data.
- "wvar": A list containing the computed wavelet variance based on the data.

**Source**

The IMU data of the navchip sensor comes from Geodetic Engineering Laboratory (TOPO) and Swiss Federal Institute of Technology Lausanne (EPFL).

---

qn_to_wv	<i>Quantisation Noise (QN) to WV</i>
----------	--------------------------------------

---

**Description**

This function compute the Haar WV of a Quantisation Noise (QN) process

**Usage**

qn\_to\_wv(q2, tau)

**Arguments**

q2	A double corresponding to variance of drift
tau	A vec containing the scales e.g. $2^{\tau}$

**Value**

A vec containing the wavelet variance of the QN.

**Process Haar Wavelet Variance Formula**

The Quantization Noise (QN) process has a Haar Wavelet Variance given by:

$$\nu_j^2(Q^2) = \frac{6Q^2}{\tau_j^2}$$

---

 robust\_eda

---

*Comparison between classical and robust Wavelet Variances*


---

**Description**

Displays a plot of the wavelet variances (classical and robust) for a given time series accounting for CI values.

**Usage**

```
robust_eda(
  x,
  eff = 0.6,
  units = NULL,
  xlab = NULL,
  ylab = NULL,
  main = NULL,
  col_wv = NULL,
  col_ci = NULL,
  nb_ticks_x = NULL,
  nb_ticks_y = NULL,
  legend_position = NULL,
  ...
)
```

**Arguments**

x	A time series objects.
eff	An integer that specifies the efficiency of the robust estimator.
units	A string that specifies the units of time plotted on the x axis.
xlab	A string that gives a title for the x axis.
ylab	A string that gives a title for the y axis.
main	A string that gives an overall title for the plot.
col_wv	A string that specifies the color of the wavelet variance line.
col_ci	A string that specifies the color of the confidence interval shade.

**nb\_ticks\_x** An integer that specifies the maximum number of ticks for the x-axis.  
**nb\_ticks\_y** An integer that specifies the maximum number of ticks for the y-axis.  
**legend\_position** A string that specifies the position of the legend (use `legend_position = NA` to remove legend).  
**...** Additional arguments affecting the plot.

**Value**

Plot of wavelet variance and confidence interval for each scale.

**Author(s)**

Stephane Guerrier, Nathanael Claussen, and Justin Lee

**Examples**

```

set.seed(999)
n = 10^4
Xt = rnorm(n)
wv = wvar(Xt)

plot(wv)
plot(wv, main = "Simulated white noise", xlab = "Scales")
plot(wv, units = "sec", legend_position = "topright")
plot(wv, col_wv = "darkred", col_ci = "pink")

```

---

 rw\_to\_wv

*Random Walk to WV*


---

**Description**

This function compute the WV (haar) of a Random Walk process

**Usage**

```
rw_to_wv(gamma2, tau)
```

**Arguments**

**gamma2** A double corresponding to variance of RW  
**tau** A vec containing the scales e.g.  $2^\tau$

**Value**

A vec containing the wavelet variance of the random walk.

**Process Haar Wavelet Variance Formula**

The Random Walk (RW) process has a Haar Wavelet Variance given by:

$$\nu_j^2(\gamma^2) = \frac{(\tau_j^2 + 2)\gamma^2}{12\tau_j}$$

---

 sarma\_objdesc

---

 Create the ts.model obj.desc given split values
 

---

**Description**

Computes the total phi and total theta vector length.

**Usage**

```
sarma_objdesc(ar, ma, sar, sma, s, i, si)
```

**Arguments**

ar	A vec containing the non-seasonal phi parameters.
ma	A vec containing the non-seasonal theta parameters.
sar	A vec containing the seasonal phi parameters.
sma	A vec containing the seasonal theta parameters.
s	An unsigned integer containing the frequency of seasonality.
i	An unsigned integer containing the number of non-seasonal differences.
si	An unsigned integer containing the number of seasonal differences.

**Value**

A vec with rows:

**np** Number of Non-Seasonal AR Terms  
**nq** Number of Non-Seasonal MA Terms  
**nsp** Number of Seasonal AR Terms  
**nsq** Number of Seasonal MA Terms  
**nsigma** Number of Variances (always 1)  
**s** Season Value  
**i** Number of non-seasonal differences  
**si** Number of Seasonal Differences

---

sp_hfilter	<i>Haar filter for a spatial case</i>
------------	---------------------------------------

---

**Description**

Haar filter for a spatial case

**Usage**

```
sp_hfilter(jscale)
```

**Arguments**

jscale	An int of the Number of Scales
--------	--------------------------------

---

sp_modwt_cpp	<i>Compute the Spatial Wavelet Coefficients</i>
--------------	---

---

**Description**

Compute the Spatial Wavelet Coefficients

**Usage**

```
sp_modwt_cpp(X, J1, J2)
```

**Arguments**

X	is a matrix with row, col orientation
J1, J2	is the levels of decomposition along the rows, columns

**Details**

By default this function will return the wavelet coefficient in addition to the wavelet

**Value**

A list of vectors containing the wavelet coefficients.

wccv

*Cross Covariance of Matrix***Description**

Calculates the Cross-covariance between multiple wavelet transformations (dwt or modwt)

**Usage**

```
wccv(x, decomp = "modwt", filter = "haar", nlevels = NULL)
```

**Arguments**

x	A vector with dimensions N x M.
decomp	A string that indicates whether to use the "dwt" or "modwt" decomposition.
filter	A string that specifies what wavelet filter to use.
nlevels	An integer that indicates the level of decomposition. It must be less than or equal to $\lfloor \log_2(\text{length}(x)) \rfloor$ .

**Details**

If nlevels is not specified, it is set to  $\lfloor \log_2(\text{length}(x)) \rfloor$

**Value**

Returns a matrix of lists of all the possible pair cross-covariance, variance of each wavelet cross-covariance and its 95

**Author(s)**

Justin Lee

wccv\_get\_y

*Mapping to log10 scale***Description**

Map x to the value in log10 scale

**Usage**

```
wccv_get_y(x, tick_y_min, tick_y_step)
```

**Arguments**

x	A vector with dimensions J x 1.
tick_y_min	A negative integer the minimum power of 10, which corresponds to the smallest scale on y-axis.
tick_y_step	An integer indicating the increment of the sequence.

**Details**

tick\_y\_min is usually chosen as  $\text{floor}(\min(\log_{10}(\text{abs}(x))))$

**Value**

A field<vec> that contains values in log10 scale.

**Author(s)**

James Balamuta and Justin Lee

**Examples**

```
x = 2^(-1:-9)
y.min = floor(min(log10(abs(x))))
y.step = 2
wccv_get_y(x, y.min, y.step)
```

---

wccv\_pair

*Cross Covariance of a TS Pair*


---

**Description**

Calculates the Cross-covariance between two wavelet transformations (dwt or modwt)

**Usage**

```
wccv_pair(x, y, decomp = "modwt", filter = "haar", nlevels = NULL)
```

**Arguments**

x	A vector with dimensions N x 1.
y	A vector with dimensions N x 1.
decomp	A string that indicates whether to use the "dwt" or "modwt" decomposition.
filter	A string that specifies what wavelet filter to use.
nlevels	An integer that indicates the level of decomposition. It must be less than or equal to $\text{floor}(\log_2(\text{length}(x)))$ .

**Details**

If `nlevels` is not specified, it is set to  $\lfloor \log_2(\text{length}(x)) \rfloor$

**Value**

Returns a list of a matrix containing cross-covariance, variance of each wavelet cross-covariance and its 95

**Author(s)**

Justin Lee

---

 wn\_to\_wv

*Gaussian White Noise to WV*


---

**Description**

This function compute the Haar WV of a Gaussian White Noise process

**Usage**

```
wn_to_wv(sigma2, tau)
```

**Arguments**

<code>sigma2</code>	A double corresponding to variance of WN
<code>tau</code>	A vec containing the scales e.g. $2^\tau$

**Value**

A vec containing the wavelet variance of the white noise.

**Process Haar Wavelet Variance Formula**

The Gaussian White Noise (WN) process has a Haar Wavelet Variance given by:

$$\nu_j^2(\sigma^2) = \frac{\sigma^2}{\tau_j^2}$$



**Description**

Calculates the (MO)DWT wavelet variance

**Usage**

```
wvar(x, ...)  
  
## S3 method for class 'lts'  
wvar(  
  x,  
  decomp = "modwt",  
  filter = "haar",  
  nlevels = NULL,  
  alpha = 0.05,  
  robust = FALSE,  
  eff = 0.6,  
  to.unit = NULL,  
  ...  
)  
  
## S3 method for class 'gts'  
wvar(  
  x,  
  decomp = "modwt",  
  filter = "haar",  
  nlevels = NULL,  
  alpha = 0.05,  
  robust = FALSE,  
  eff = 0.6,  
  to.unit = NULL,  
  ...  
)  
  
## S3 method for class 'ts'  
wvar(  
  x,  
  decomp = "modwt",  
  filter = "haar",  
  nlevels = NULL,  
  alpha = 0.05,  
  robust = FALSE,  
  eff = 0.6,  
  to.unit = NULL,
```

```

    ...
)

## S3 method for class 'imu'
wvar(
  x,
  decomp = "modwt",
  filter = "haar",
  nlevels = NULL,
  alpha = 0.05,
  robust = FALSE,
  eff = 0.6,
  to.unit = NULL,
  ...
)

## Default S3 method:
wvar(
  x,
  decomp = "modwt",
  filter = "haar",
  nlevels = NULL,
  alpha = 0.05,
  robust = FALSE,
  eff = 0.6,
  freq = 1,
  from.unit = NULL,
  to.unit = NULL,
  ...
)

```

### Arguments

<code>x</code>	A vector with dimensions $N \times 1$ .
<code>...</code>	Further arguments passed to or from other methods.
<code>decomp</code>	A string that indicates whether to use a "dwt" or "modwt" decomposition.
<code>filter</code>	A string that specifies which wavelet filter to use.
<code>nlevels</code>	An integer that indicates the level of decomposition. It must be less than or equal to $\text{floor}(\log_2(\text{length}(x)))$ .
<code>alpha</code>	A double that specifies the significance level which in turn specifies the $1 - \alpha$ confidence level.
<code>robust</code>	A boolean that triggers the use of the robust estimate.
<code>eff</code>	A double that indicates the efficiency as it relates to an MLE.
<code>to.unit</code>	A string indicating the unit to which the data is converted.
<code>freq</code>	A numeric that provides the rate of samples.
<code>from.unit</code>	A string indicating the unit from which the data is converted.

**Details**

The default value of `nlevels` will be set to  $\lceil \log_2(\text{length}(x)) \rceil$ , unless otherwise specified.

**Value**

A list with the structure:

- "variance": Wavelet Variance
- "ci\_low": Lower CI
- "ci\_high": Upper CI
- "robust": Robust active
- "eff": Efficiency level for Robust calculation
- "alpha": p value used for CI
- "unit": String representation of the unit

**Author(s)**

James Balamuta, Justin Lee and Stephane Guerrier

**Examples**

```
set.seed(999)
x = rnorm(100)

# Default
wvar(x)

# Robust
wvar(x, robust = TRUE, eff=0.3)

# Classical
wvar(x, robust = FALSE, eff=0.3)

# 90% Confidence Interval
wvar(x, alpha = 0.10)
```

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