

Package ‘EvolutionaryGames’

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Type Package

Title Important Concepts of Evolutionary Game Theory

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Description A comprehensive set of tools to illustrate the core concepts of evolutionary game theory, such as evolutionary stability or various evolutionary dynamics, for teaching and academic research.

License GPL-2

Encoding UTF-8

LazyData true

Imports deSolve (>= 1.14), geometry (>= 0.3-6), ggplot2 (>= 2.2.1), grDevices (>= 3.2.2), interp (>= 1.0-29), MASS (>= 7.3-43), reshape2 (>= 1.4.2), rgl (>= 0.95.1201)

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| | |
|-----|---------------------------------------|
| BNN | <i>Brown-von Neumann-Nash dynamic</i> |
|-----|---------------------------------------|

Description

Brown-von Neumann-Nash replicator dynamic as a type of evolutionary dynamics.

Usage

```
BNN(time, state, parameters)
```

Arguments

| | |
|------------|--|
| time | Regular sequence that represents the time sequence under which simulation takes place. |
| state | Numeric vector that represents the initial state. |
| parameters | Numeric vector that represents parameters needed by the dynamic. |

Value

Numeric list. Each component represents the rate of change depending on the dynamic.

Author(s)

Daniel Gebele <dngebele@gmail.com>

References

Brown, G. W. and von Neumann, J. (1950) "Solutions of games by differential equations", In: Kuhn, Harold William and Tucker, Albert William (Eds.) "Contributions to the Theory of Games I", Princeton University Press, pp. 73–79.

Examples

```
dynamic <- BNN
A <- matrix(c(0, -2, 1, 1, 0, -2, -2, 1, 0), 3, byrow=TRUE)
state <- matrix(c(0.4, 0.3, 0.3), 1, 3, byrow=TRUE)
phaseDiagram3S(A, dynamic, NULL, state, FALSE, FALSE)
```

| | |
|----|-------------------|
| BR | <i>BR dynamic</i> |
|----|-------------------|

Description

Best response dynamic as a type of evolutionary dynamics.

Usage

```
BR(time, state, parameters)
```

Arguments

| | |
|------------|--|
| time | Regular sequence that represents the time sequence under which simulation takes place. |
| state | Numeric vector that represents the initial state. |
| parameters | Numeric vector that represents parameters needed by the dynamic. |

Value

Numeric list. Each component represents the rate of change depending on the dynamic.

Author(s)

Daniel Gebele <dngebele@gmail.com>

References

Gilboa, I. and Matsui, A. (1991) "Social Stability and Equilibrium", *Econometrica* 59, pp. 859–867.

Examples

```
dynamic <- BR
A <- matrix(c(0, -2, 1, 1, 0, -2, -2, 1, 0), 3, byrow=TRUE)
state <- matrix(c(0.4, 0.3, 0.3), 1, 3, byrow=TRUE)
phaseDiagram3S(A, dynamic, NULL, state, FALSE, FALSE)
```

ESS

ESS for two-player games with a maximum of three strategies

Description

Computes Evolutionary Stable Strategies of a game with two players and a maximum of three strategies.

Usage

```
ESS(A, strategies = c(), floats = TRUE)
```

Arguments

| | |
|------------|---|
| A | Numeric matrix of size 2x2 or 3x3 representing the number of strategies of a symmetric matrix game. |
| strategies | String vector of length n that names all strategies whereas n represents the number of strategies. |
| floats | Logical value that handles number representation. If set to TRUE, floating-point arithmetic will be used, otherwise fractions. Default is TRUE. |

Value

Numeric matrix. Each row represents an ESS.

Author(s)

Daniel Gebele <dngebele@gmail.com>

References

Smith, J. M. and Price, G. R. (1973) "The logic of animal conflict", Nature 246, pp. 15–18.

Examples

```
ESS(matrix(c(-1, 4, 0, 2), 2, byrow=TRUE), c("Hawk", "Dove"), FALSE)
ESS(matrix(c(1, 2, 0, 0, 1, 2, 2, 0, 1), 3, byrow=TRUE))
```

ESset

Evolutionarily stable set for two-player games with three strategies

Description

Computes evolutionarily stable sets of a game with two players and three strategies.

Usage

```
ESset(A, strategies = c("1", "2", "3"), floats = TRUE)
```

Arguments

| | |
|------------|---|
| A | Numeric matrix of size 3x3 representing the number of strategies of a symmetric matrix game. |
| strategies | String vector of length 3 that names all strategies. |
| floats | Logical value that handles number representation. If set to TRUE, floating-point arithmetic will be used, otherwise fractions. Default is TRUE. |

Value

Numeric matrix. Each row represents the start and end point of a line (ESset). In addition, a plot of the ESset in the game will be created.

Author(s)

Daniel Gebele <dngebele@gmail.com>

References

Thomas, B. (1985) "On evolutionarily stable sets", *Journal of Mathematical Biology* 22, pp. 105–115.

Examples

```
# Please note that the computation of evolutionarily stable sets
# is rather time-consuming.
# Depending on your machine you might need to wait more
# than 10 seconds in order to run the following example.
## Not run:
A <- matrix(c(-2, 5, 10/9, 0, 5/2, 10/9, -10/9, 35/9, 10/9), 3, byrow=TRUE)
strategies <- c("Hawk", "Dove", "Mixed ESS")
ESset(A, strategies)

## End(Not run)
```

ILogit

ILogit dynamic

Description

Imitative Logit dynamic as a type of evolutionary dynamics.

Usage

```
ILogit(time, state, parameters)
```

Arguments

| | |
|------------|--|
| time | Regular sequence that represents the time sequence under which simulation takes place. |
| state | Numeric vector that represents the initial state. |
| parameters | Numeric vector that represents parameters needed by the dynamic. |

Value

Numeric list. Each component represents the rate of change depending on the dynamic.

Author(s)

Jochen Staudacher <jochen.staudacher@hs-kempten.de>

References

Weibull, J. W. (1997) "Evolutionary Game Theory", MIT Press.

Examples

```
dynamic <- ILogit
A <- matrix(c(-1, 0, 0, 0, -1, 0, 0, 0, -1), 3, byrow=TRUE)
state <- matrix(c(0.1, 0.2, 0.7, 0.2, 0.7, 0.1, 0.9, 0.05, 0.05), 3, 3, byrow=TRUE)
eta <- 0.7
phaseDiagram3S(A, dynamic, eta, state, TRUE, FALSE)
```

Logit

Logit dynamic

Description

Logit dynamic as a type of evolutionary dynamics.

Usage

```
Logit(time, state, parameters)
```

Arguments

| | |
|------------|--|
| time | Regular sequence that represents the time sequence under which simulation takes place. |
| state | Numeric vector that represents the initial state. |
| parameters | Numeric vector that represents parameters needed by the dynamic. |

Value

Numeric list. Each component represents the rate of change depending on the dynamic.

Author(s)

Daniel Gebele <dngebele@gmail.com>

References

Fudenberg, D. and Levine, D. K. (1998) "The Theory of Learning in Games", MIT Press.

Examples

```
dynamic <- Logit
A <- matrix(c(0, -2, 1, 1, 0, -2, -2, 1, 0), 3, byrow=TRUE)
state <- matrix(c(0.4, 0.3, 0.3), 1, 3, byrow=TRUE)
eta <- 0.1
phaseDiagram3S(A, dynamic, eta, state, FALSE, FALSE)
```

| | |
|--------------|---|
| MSReplicator | <i>Maynard Smith replicator dynamic</i> |
|--------------|---|

Description

Maynard Smith replicator dynamic as a type of evolutionary dynamics.

Usage

```
MSReplicator(time, state, parameters)
```

Arguments

| | |
|------------|--|
| time | Regular sequence that represents the time sequence under which simulation takes place. |
| state | Numeric vector that represents the initial state. |
| parameters | Numeric vector that represents parameters needed by the dynamic. |

Value

Numeric list. Each component represents the rate of change depending on the dynamic.

Author(s)

Daniel Gebele <dngebele@gmail.com>

References

Smith, J. M. (1982) "Evolution and the Theory of Games", Cambridge University Press.

Examples

```
dynamic <- MSReplicator
A <- matrix(c(0, -2, 1, 1, 0, -2, -2, 1, 0), 3, byrow=TRUE)
state <- matrix(c(0.4, 0.3, 0.3), 1, 3, byrow=TRUE)
phaseDiagram3S(A, dynamic, NULL, state, FALSE, FALSE)
```

phaseDiagram2S *Phase Diagram for two-player games with two strategies*

Description

Plots phase diagram of a game with two players and two strategies.

Usage

```
phaseDiagram2S(A, dynamic, params = NULL, vectorField = TRUE,  
  strategies = c("1", "2"))
```

Arguments

| | |
|-------------|---|
| A | Numeric matrix of size 2x2 representing the number of strategies of a symmetric matrix game. |
| dynamic | Function representing an evolutionary dynamic. |
| params | Numeric vector representing additional parameters for the evolutionary dynamic. |
| vectorField | Logical value that handles vector field presentation. If set to TRUE, vector field will be shown, otherwise not. Default is TRUE. |
| strategies | String vector of length 2 that names all strategies. |

Value

None.

Author(s)

Daniel Gebele <dngebele@gmail.com>

Examples

```
A <- matrix(c(-1, 4, 0, 2), 2, 2, byrow=TRUE)  
phaseDiagram2S(A, Replicator, strategies = c("Hawk", "Dove"))
```

 phaseDiagram3S

Phase Diagram for two-player games with three strategies

Description

Plots phase diagram of a game with two players and three strategies.

Usage

```
phaseDiagram3S(A, dynamic, params = NULL, trajectories = NULL,
  contour = FALSE, vectorField = FALSE, strategies = c("1", "2", "3"))
```

Arguments

| | |
|--------------|--|
| A | Numeric matrix of size 3x3 representing the number of strategies of a symmetric matrix game. |
| dynamic | Function representing an evolutionary dynamic. |
| params | Numeric vector with additional parameters for the evolutionary dynamic. |
| trajectories | Numeric matrix of size mx3. Each row represents the initial values for the trajectory to be examined. |
| contour | Logical value that handles contour diagram presentation. If set to TRUE, contour diagram will be shown, otherwise not. Default is FALSE. |
| vectorField | Logical value that handles vector field presentation. If set to TRUE, vector field will be shown, otherwise not. Default is FALSE. |
| strategies | String vector of length 3 that names all strategies. |

Value

None.

Author(s)

Daniel Gebele <dngbele@gmail.com>

Examples

```
A <- matrix(c(0, -2, 1, 1, 0, -2, -2, 1, 0), 3, byrow=TRUE)
state <- matrix(c(0.4, 0.3, 0.3), 1, 3, byrow=TRUE)

phaseDiagram3S(A, Replicator, NULL, state, FALSE, FALSE)
phaseDiagram3S(A, Replicator, NULL, state, TRUE, TRUE)

# Plot two trajectories rather than only one:
A <- matrix(c(0, -2, 1, 1, 0, -2, -2, 1, 0), 3, byrow=TRUE)
state <- matrix(c(0.4, 0.3, 0.3, 0.6, 0.2, 0.2), 2, 3, byrow=TRUE)
phaseDiagram3S(A, Replicator, NULL, state, FALSE, FALSE)
```

`phaseDiagram4S`*Phase Diagram for two-player games with four strategies*

Description

Plots phase diagram of a game with two players and four strategies.

Usage

```
phaseDiagram4S(A, dynamic, params = NULL, trajectory = NULL,  
  strategies = c("1", "2", "3", "4"), noRGL = TRUE)
```

Arguments

| | |
|-------------------------|--|
| <code>A</code> | Numeric matrix of size 4x4 representing the number of strategies of a symmetric matrix game. |
| <code>dynamic</code> | Function representing an evolutionary dynamic. |
| <code>params</code> | Numeric vector with additional parameters for the evolutionary dynamic. |
| <code>trajectory</code> | Numeric vector of size 4 representing the initial value for the trajectory to be examined. |
| <code>strategies</code> | String vector of length 4 that names all strategies. |
| <code>noRGL</code> | Logical value that handles diagram rotation. If set to FALSE, diagram will be rotatable, otherwise not. Default is TRUE. |

Value

None.

Author(s)

Daniel Gebele <dngebele@gmail.com>

Examples

```
A <- matrix(c(5, -9, 6, 8, 20, 1, 2, -18, -14, 0, 2, 20, 13, 0, 4, -13),  
  4, 4, byrow=TRUE)  
state <- c(0.3, 0.2, 0.1, 0.4)  
phaseDiagram4S(A, Replicator, NULL, state)
```

| | |
|------------|---------------------------|
| Replicator | <i>Replicator dynamic</i> |
|------------|---------------------------|

Description

Replicator dynamic as a type of evolutionary dynamics.

Usage

```
Replicator(time, state, parameters)
```

Arguments

| | |
|------------|--|
| time | Regular sequence that represents the time sequence under which simulation takes place. |
| state | Numeric vector that represents the initial state. |
| parameters | Numeric vector that represents parameters needed by the dynamic. |

Value

Numeric list. Each component represents the rate of change depending on the dynamic.

Author(s)

Daniel Gebele <dngebele@gmail.com>

References

Taylor, P. D. and Jonker, L. B. (1978) "Evolutionary stable strategies and game dynamics", *Mathematical Biosciences* 40 (1-2), pp. 145–156.

Examples

```
dynamic <- Replicator
A <- matrix(c(0, -2, 1, 1, 0, -2, -2, 1, 0), 3, byrow=TRUE)
state <- matrix(c(0.4, 0.3, 0.3), 1, 3, byrow=TRUE)
phaseDiagram3S(A, dynamic, NULL, state, FALSE, FALSE)
```

| | |
|-------|----------------------|
| Smith | <i>Smith dynamic</i> |
|-------|----------------------|

Description

Smith dynamic as a type of evolutionary dynamics.

Usage

```
Smith(time, state, parameters)
```

Arguments

| | |
|------------|--|
| time | Regular sequence that represents the time sequence under which simulation takes place. |
| state | Numeric vector that represents the initial state. |
| parameters | Numeric vector that represents parameters needed by the dynamic. |

Value

Numeric list. Each component represents the rate of change depending on the dynamic.

Author(s)

Daniel Gebele <dngebele@gmail.com>

References

Smith, M. J. (1984) "The Stability of a Dynamic Model of Traffic Assignment – An Application of a Method of Lyapunov", *Transportation Science* 18, pp. 245–252.

Examples

```
dynamic <- Smith
A <- matrix(c(0, -2, 1, 1, 0, -2, -2, 1, 0), 3, byrow=TRUE)
state <- matrix(c(0.4, 0.3, 0.3), 1, 3, byrow=TRUE)
phaseDiagram3S(A, dynamic, NULL, state, FALSE, FALSE)
```

| | |
|----------|--|
| triangle | <i>Triangle for 2-simplex operations</i> |
|----------|--|

Description

Generates a triangle representing the 2-simplex.

Usage

```
triangle(labels = c("1", "2", "3"))
```

Arguments

labels String vector of length 3 that names the edges of the triangle.

Value

List of size 2 with members coords and canvas. coords holds edge coordinates of the 2-simplex, canvas a ggplot2 plot object of the 2-simplex.

Author(s)

Daniel Gebele <dngebele@gmail.com>

Examples

```
triangle()
```

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